

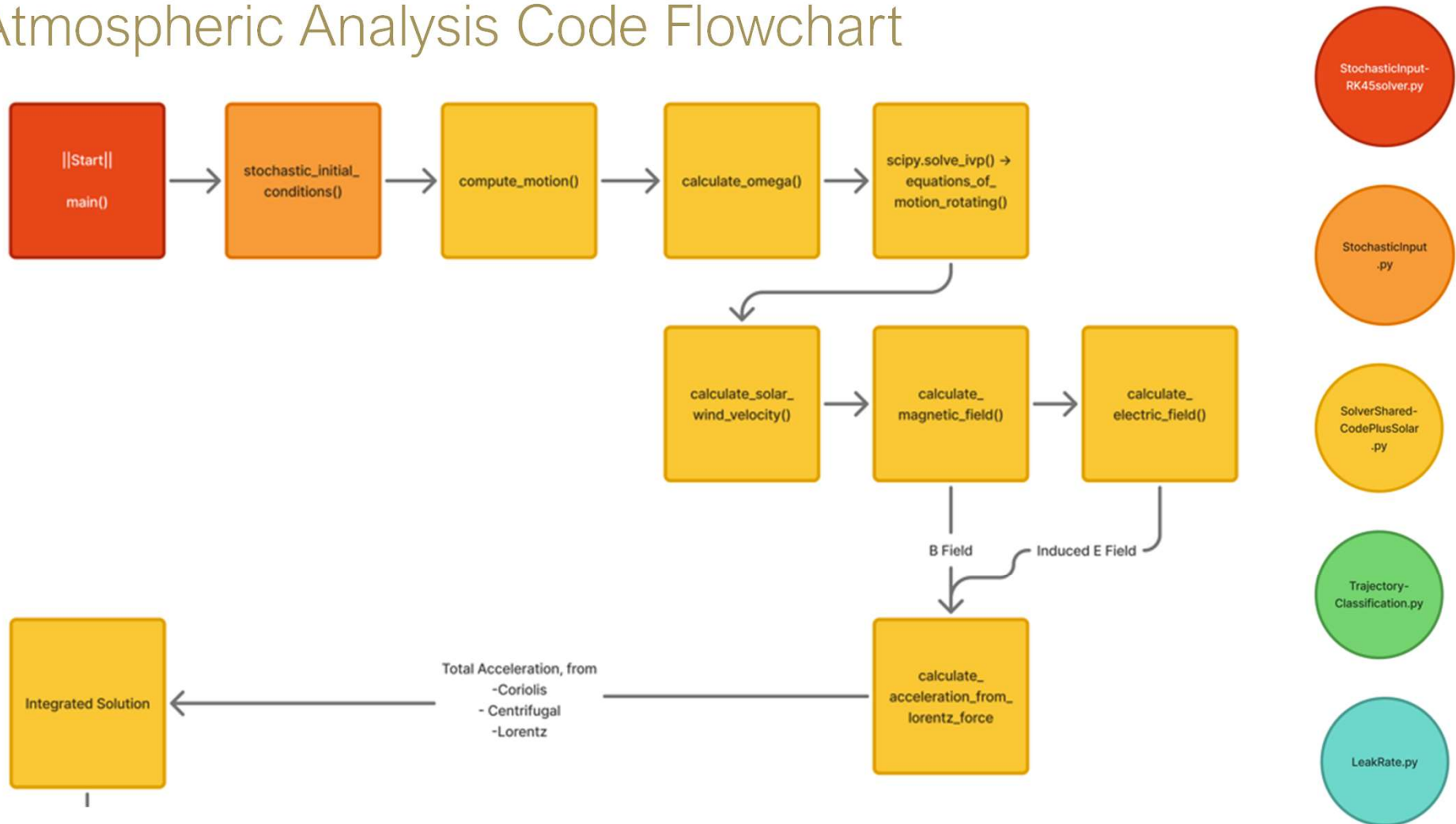
Ringworld research presentation

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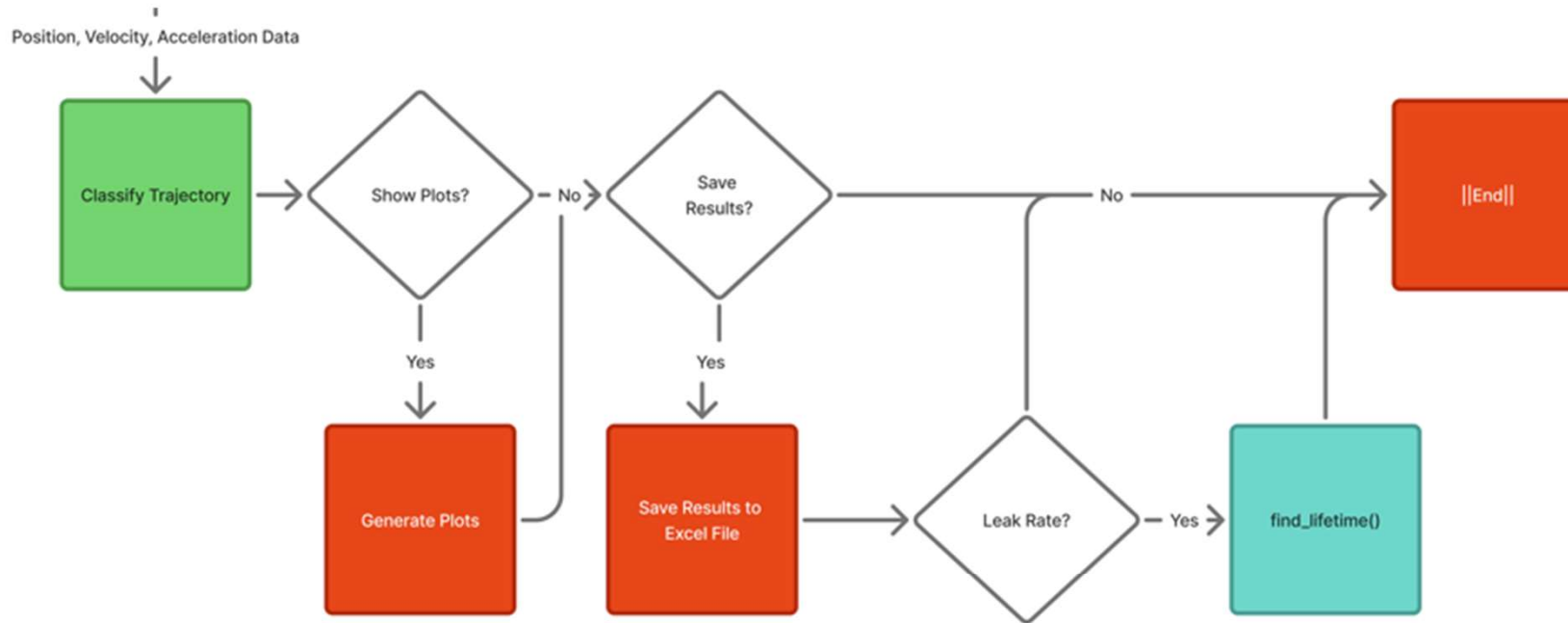
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December 1, 2025

Atmospheric Analysis Code Flowchart



Atmospheric Analysis Code Flowchart (cont.)



StochasticInput-
RK45solver.py

StochasticInput
.py

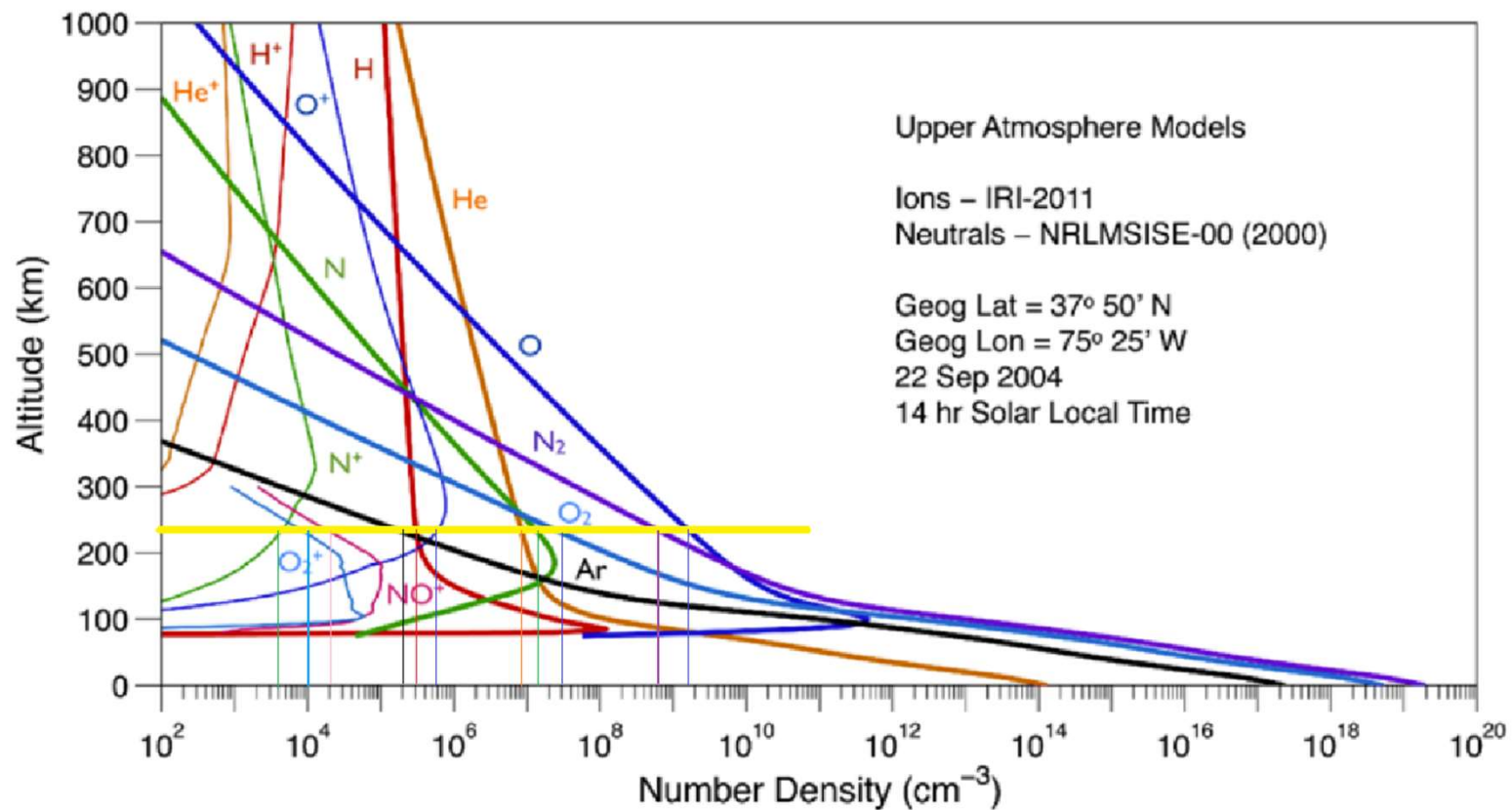
SolverShared-
CodePlusSolar
.py

Trajectory-
Classification.py

LeakRate.py

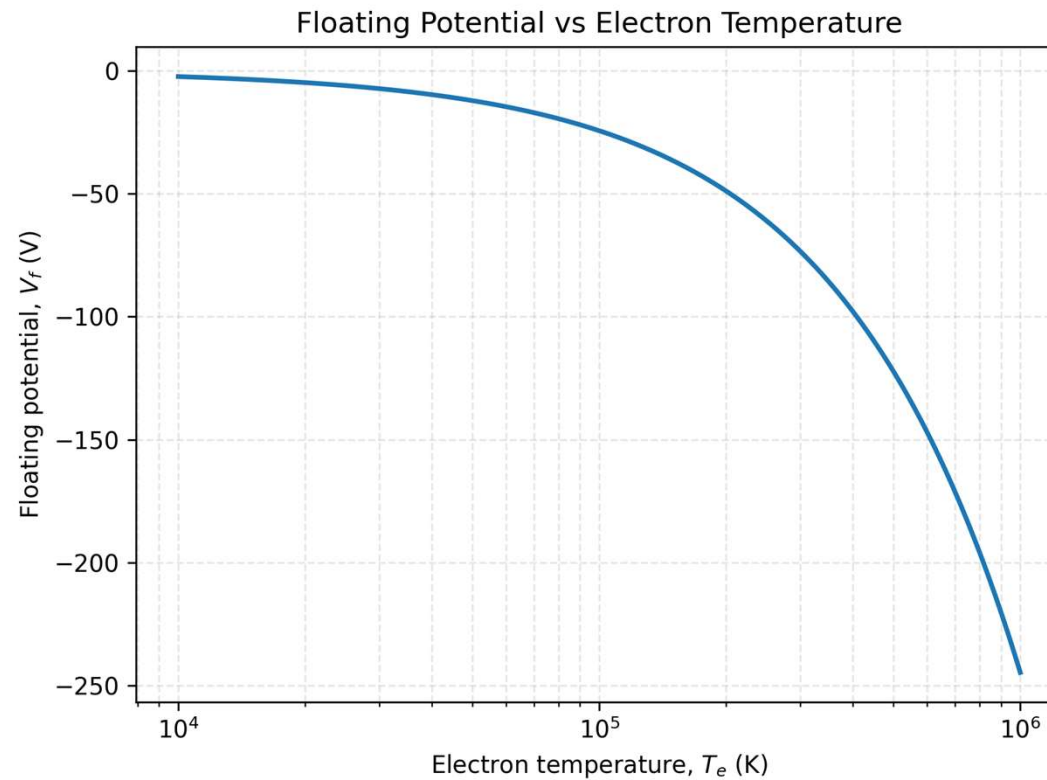
Atmosphere Composition

- The composition for the atmosphere was modelled off the Earth's atmosphere at an altitude of 218km.



Floating Potential

- Floating potentials were calculated over a range of temperatures and found to be negligible because of the Ringworld's scale.



Electromagnetic Effects of Solar Wind

Solar Wind Magnetic Field

B_{r0} is magnetic field at Earth's location, r_0 is the distance from the Earth to the Sun, v_r is solar wind speed and ω is angular speed

$$B_r(r) = B_{r0} \left(\frac{r_0}{r} \right)^2 \quad B_\phi(r) = - \frac{\omega r B_r}{v_r}$$
$$B = \langle B_r, 0, B_\phi \rangle$$

Solar Wind Electric Field

The `inertial_to_rotating` function is used to convert from inertial frame to rotating frame for the solar wind velocity.

$$v_r = \langle v_r, 0, 0 \rangle_r$$

$$v_{inertial} = v_r \frac{r}{r_{mag}}$$

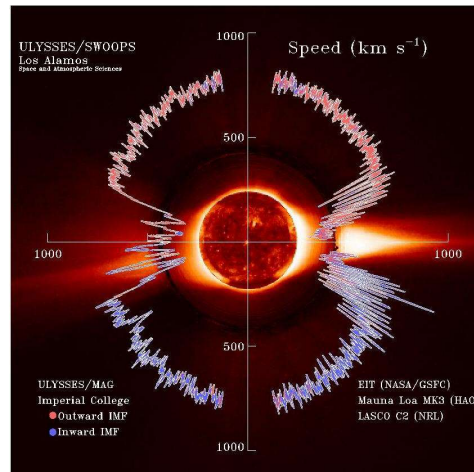
$$v_{rotating} = \text{inertial_to_rotating}(v_{inertial})$$

$$\omega = \langle 0, 0, \omega \rangle$$

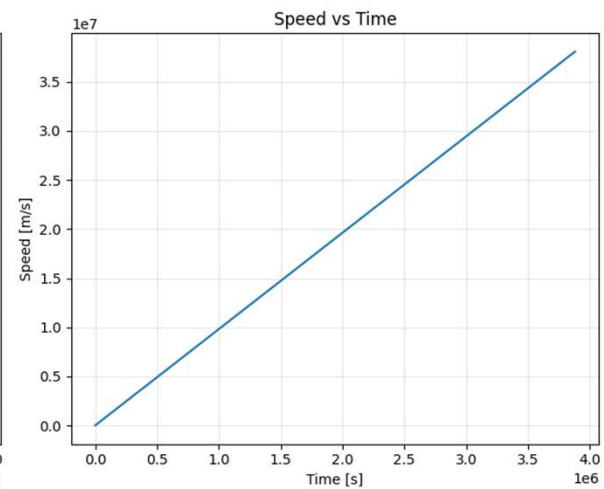
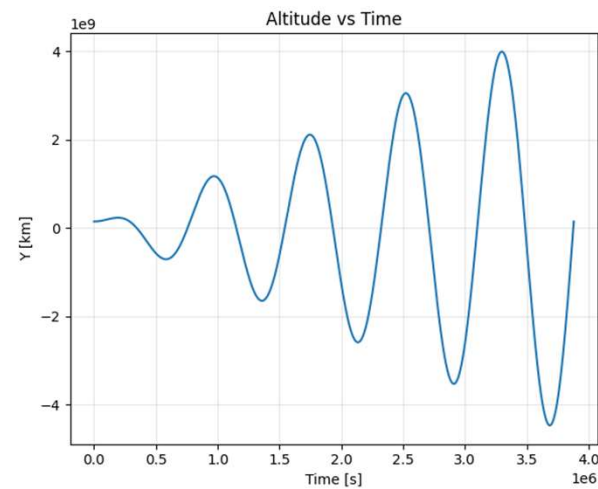
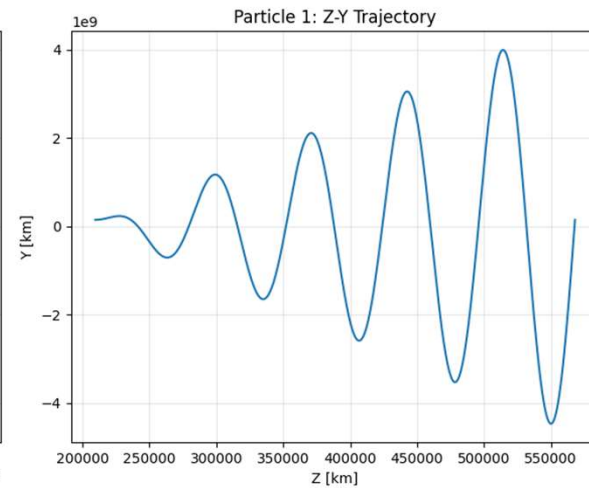
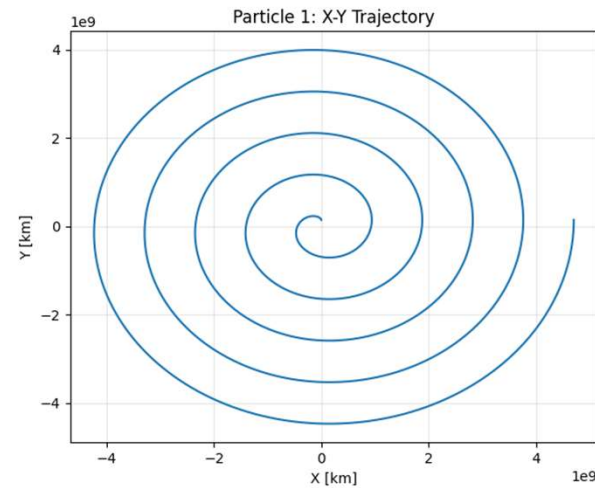
$$v_{combined} = v_{rotating} - \omega r$$

$$E = -v \times B$$

The solar wind speed was computed using this polar plot from the Ulysses results.



Trajectory Graphs of Particles



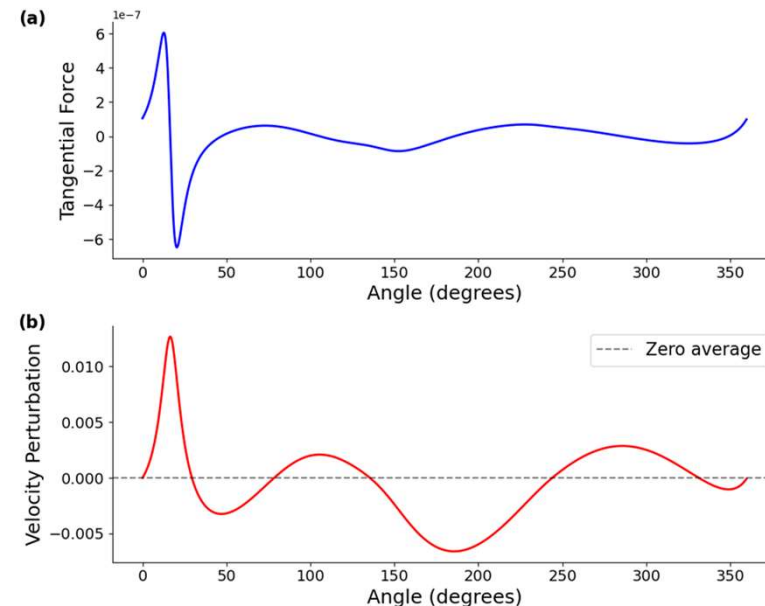
Third-Body Gravity Graphs

A simulation of gravity effects from third-body objects is conducted.

Gravity from third-body objects:

$$G \cdot \frac{m_1 \mathbf{d}}{|\mathbf{d}|^3} - G \cdot \frac{m_1 \mathbf{r}}{|\mathbf{r}|^3}$$

- m_1 is the mass of the the third-body object
- \mathbf{d} is the vector distance between the center of the Ringworld and the third-body object
- \mathbf{r} is the position of the center of the Ringworld.



PBL Wind Modeling

- Evaluated two boundary-layer velocity profiles:

Power-law: $U(z) = U_{\text{ref}} \left(\frac{z}{z_{\text{ref}}} \right)^{\alpha}$

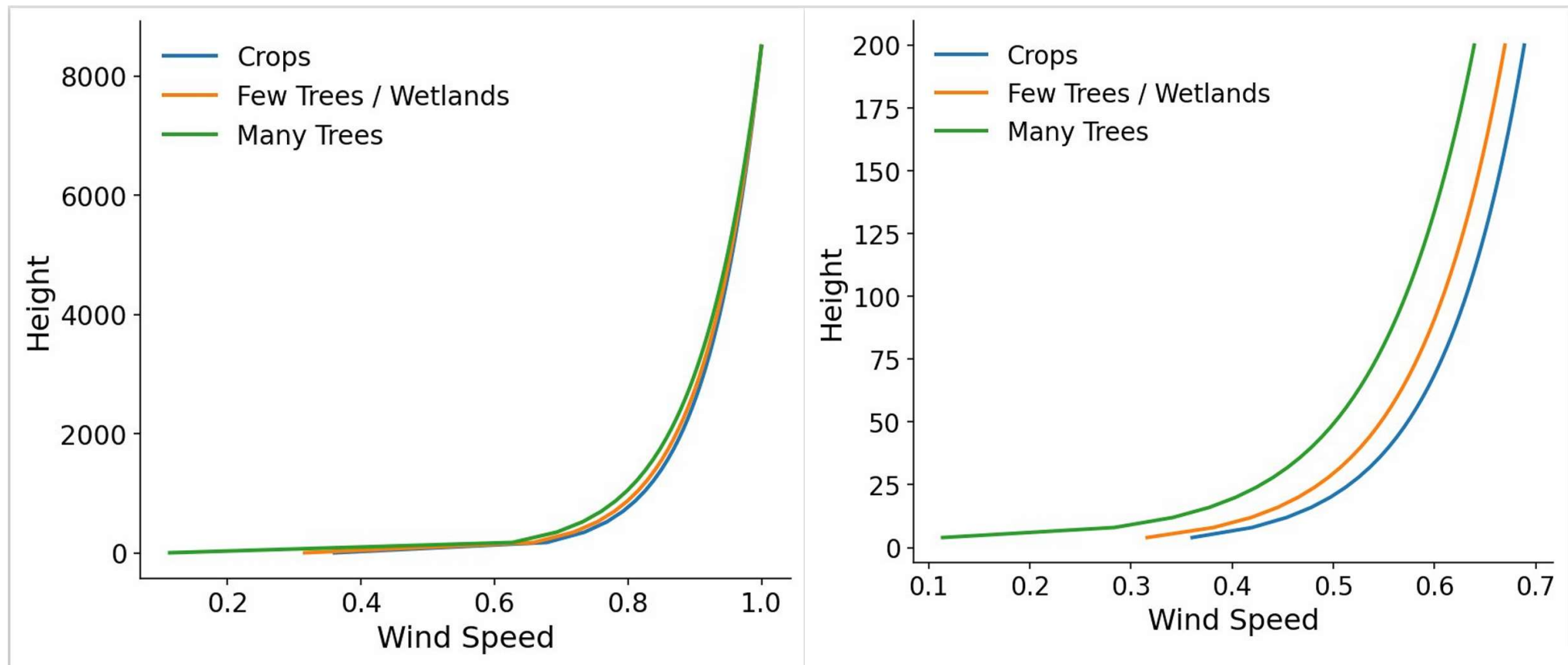
Log-law: $U(z) = \frac{u_*}{\kappa} \ln \left(\frac{z-d}{z_0} \right)$

- Chose the log-law because it represents heterogeneous terrain more realistically and avoids the power-law's monotonic assumptions.
- Generated two wind-speed curves for each surface type:

Surface Type	z_0 (m)	d (m)
Crops	0.05	0.16
Few trees / Wetlands	0.10	0.39
Many trees	0.25	3.18

0–200 m to capture near-surface PBL structure,
0–8500 m to scale up toward atmospheric height.

Normalized log-law velocity profiles for the three surface roughness categories across the two simulated domains



Statistical Correlations

=== Normal Model ===

OLS Regression Results

```
=====
Dep. Variable:          y      R-squared:          0.983
Model:                  OLS    Adj. R-squared:      0.981
Method:                 Least Squares    F-statistic:      375.3
Date:                  Mon, 01 Dec 2025    Prob (F-statistic):  4.41e-17
Time:                  09:16:47    Log-Likelihood:     15.490
No. Observations:      23    AIC:              -22.98
Df Residuals:          19    BIC:              -18.44
Df Model:               3
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	0.8513	0.134	6.357	0.000	0.571	1.132
x1	-0.5909	0.058	-10.116	0.000	-0.713	-0.469
x2	-1.0390	0.032	-32.400	0.000	-1.106	-0.972
x3	0.0306	0.017	1.846	0.081	-0.004	0.065

```
=====
Omnibus:                11.846    Durbin-Watson:          2.487
Prob(Omnibus):           0.003    Jarque-Bera (JB):       20.340
Skew:                   -0.632    Prob(JB):               3.83e-05
Kurtosis:                7.430    Cond. No.:              40.4
=====
```

Key Model Results

- $R^2 = 0.983 \rightarrow$ strong model fit
- Adj. $R^2 = 0.981$
- F-statistic $p = 4.41 \times 10^{-17} \rightarrow$ model is statistically significant

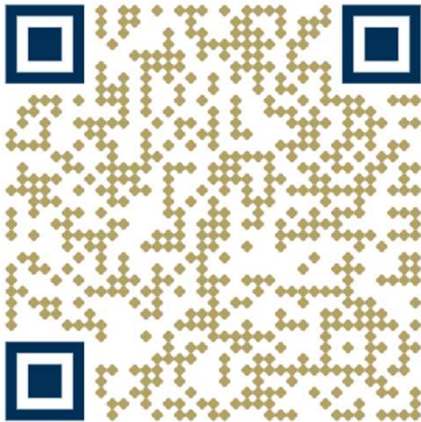
Coefficient Significance

- Gravity (x1): -0.591 , very significant ($p \sim 0$)
- Width (x2): -1.039 , very significant ($p \sim 0$)
- Radius (x3): 0.031 , weakly significant ($p = 0.081$)
- Intercept = 0.851 (baseline \log_{10} escape rate)

Interpretation

- Higher **gravity** \rightarrow lower escape probability
- Larger **width** \rightarrow lower escape probability
- Radius has minimal effect in this dataset

Questions?



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More information available at lowgravitylab.ae.gatech.edu

Backup: E-field plot

